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# ANTENNAS ARRAY ADJUST WITH ADAPTIVE NEURONAL SYSTEM

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## ABSTRACT

In this work an array failure correction for Linear Antenna Array (LAA) is presented. This is carried out by means of an Adaptive Artificial Neural Network (AANN) that adjusts the amplitude and phase at beamforming. The appropriated corrections are given, when one, or two, or three elements have a failure in the antenna linear array. The AANN corrects the corresponding parameters in the radiation pattern obtained due to the failure, when we know the coefficients of the array factor (AF). This yields a reduction of side lobe level and some interferences disappear.

## RESUMEN

En este trabajo se realiza una corrección de fallas para un Arreglo Lineal de Antenas (ALA). Esto se lleva a cabo mediante una Red Neuronal Artificial Adaptable (RNAA) que ajusta al generador del haz "beamforming" en amplitud y fase. Las pertinentes correcciones se dan, cuando en el arreglo lineal de antenas fallan uno, dos y hasta tres elementos. La RNAA corrige los debidos parámetros en el patrón de radiación obtenido para la falla, dados los coeficientes del Factor de Arreglo (AF).

**KEYWORDS:** Adaptive Artificial Neural Networks (AANN), Array Factor (AF), Side Lobe Level (SLL), Linear Antenna Array (LAA)

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## 1. INTRODUCTION

For a Linear Antenna Array with its traditional beam generator, if one or more elements are damaged by an unfortunate reason, the LAA would stop operating due to an unacceptable distortion on its radiation pattern, for example a significant increment may exist in the side lobes level (SLL). By means of the AANN it is possible not to replace the damaged element, but by recalculating the radiation pattern's parameters with the spare elements to approximate the new pattern to the original one. This capacity to correct the failure in the radiation pattern of the AANN produces a cost-effective alternative to hardware replacement which might be time-consuming, especially for arrays performing critical operations. Other applications include satellite or extraterrestrial communications (earth-air-earth) for example in spaceships, where a damaged antenna element could not be replaced easily by means of substitution [1]. In the literature no analytic technique has been devised to yield a set of new beamforming weights that effectively corrects the damaged pattern. Thus, a failure array LAA can be visualized as an non-uniformly spaced array, the analytic approaches are unable to solve this type of problems. In past years, many algorithms have been proposed to correct the damaged patterns, however, due to the outage of the geometric distribution of the spare elements in the array and the way of the wanted beamforming, the correction of the failure is still been solved by numerical approaches [2].

The adaptive arrays have been used mainly for the beamforming and to direct the null ones in several civil and military systems, including the GPS, cellular and mobile communications. The main idea in each case is to determine the angle of reception of arrival of the desired signals, as well as the directions of interfering or jamming signals. Once all these signals have been determined, the elements of the adaptive array antenna are excited with the appropriate inputs to place null in the direction of the interfering signals and beams in the desired direction. This is accomplished by finding a cost function that allows maximum gain in the directions of the desired signal and the rejection of the interference by minimizing the antenna power where it is necessary. After mathematical calculations, the cost function can be reformulated so that the optimization can be made by means of Artificial Neuronal Networks with the aim of estimating the appropriated array element weights [3].

The neural generators have the advantage of fast convergence rate that can easily allow the antenna to track the mobile user. Other problems associated with generators with the conventional beamforming stem from the requirements of highly calibrated antennas that assume identical element properties. The degradation often occurs due to the fact that this algorithms have a poor adaptation to the element failure or other sources of errors like interferences. An AANN can be trained with a number of observations of the antenna behavior under a specific set of circumstances. The net can be generalized and then it can be used to predict the aperture behavior at all points.

The LAA can be designed to control its radiation characteristics by selecting the appropriate distribution of phase and amplitude among the elements of the array. It has been proven that the phase control can significantly alter the radiation pattern of a LAA. In fact, the principle of the antennas, where the maximum pattern of the array can be aimed in different directions, is mainly based on the phase control of the elements excitement. Likewise, it has been demonstrated that an appropriate decrease on the excitement of the amplitude among the elements can be used to control the beam width and the side lobes level [4].

The Adaptive Neuronal System carries out the appropriate correction of the beamforming and generates the radiation pattern of a linear array antenna when a failure is presented in one of the elements. This system estimates the proper weights for the new amplitude and phase conditions of the beam generator. These adjustments or corrections can be clearly visualized in figure 1 [5].

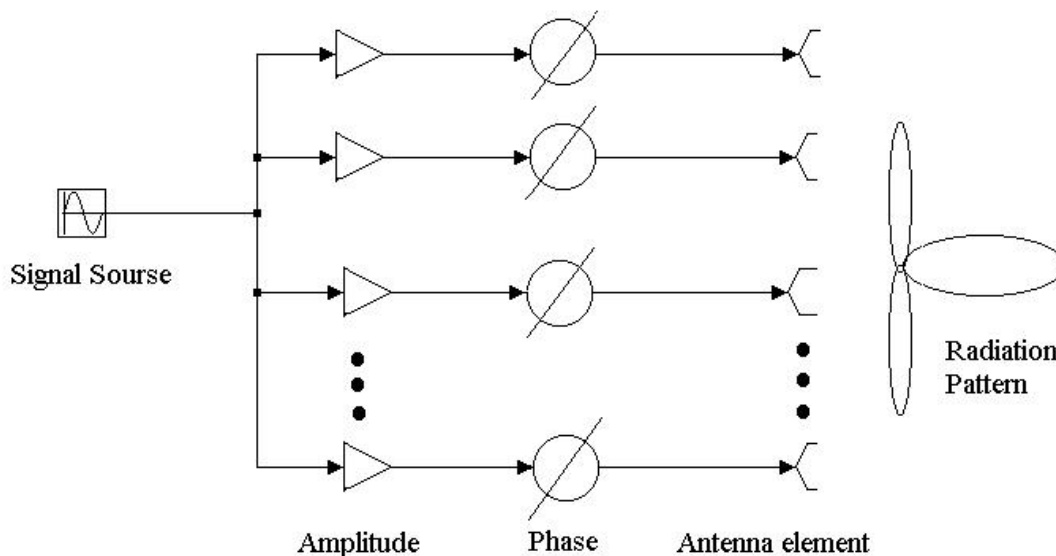


Figure 1. The Beamforming of a linear array antenna

## 2. PROBLEM FORMULATION

The beamforming of a LAA, can be used only for amplitude, for phase or amplitude-phase approach. In the case of amplitude approach it cannot compensate for the degradation of a damaged array pattern, as the failing elements introduce an asymmetrical aperture distribution. On the other hand, the case of the phase approach with constant amplitude requires a large number of elements to yield low side lobes. Consequently, beamforming using, both amplitude and phase is necessary for the redistribution of the weights, in order to correct the damaged pattern [6].

For an arbitrary arrangement, the Array Factor (AF) can generally be given by:

$$AF = W^T S(\theta, \theta_m) \quad , \quad (1)$$

where

$$W = \{w_1, w_2, \dots, w_N\}^T, \quad w_n \in \mathbb{C}^n \quad (2)$$

is the weighting vector,  $S$  the steering vector,  $\theta$  y  $\theta_m$  are the direction variables and main beam direction, respectively.  $\mathbb{C}^n$  is the set or a subset of all complex numbers.

Take, for example, a linear array of  $N$  identical elements, its steering vector is given by:

$$S = \exp \left\{ jkd \left( n - \frac{N-1}{2} \right) (\cos \theta - \cos \theta_m) \right\} \quad (3)$$

in such a way that the same set of optimum weights for the main beam at broadside can be used for other directions, when the above  $S$  vector is recalculated for the new beam-pointing direction.

When the  $M$ th-element fails in the array, its weight  $w_m$  is supposed to be similar to zero. Thereafter, the AANN is applied to correct the SLL and the main beam shape of the pattern taking in to account the previously specified failures.

## 3. ADAPTATIVE ARTIFICIAL NEURAL NETWORK

The networks with adaptive linear neurons (ADALINE) are similar to the perceptron, but their activation function is linear compared with the step or "hard limiter." This allows their outputs to take any value, whereas the perceptron output can only take values between 0 and 1. Both, the ADALINE and the perceptron can only solve linearly separable problems. However, making use of the least mean square (LMS) learning rule, which is much more powerful than the perceptron learning rule, it is possible to minimize the mean square error and thus to move the decisions boundaries as far as it can from the training patterns [7].

In an adaptive neural network when a set of input vectors is presented, produces outputs of corresponding objective or target vectors. For each input vector we can calculate the network output vector. The difference between an output vector and its target vector is the error. We would like to find values for the networks weights and bias such that the sum of the squares of the errors is minimized or below a specific value. This problem is manageable because linear systems have a single error minimum. In most cases we can calculate a linear network directly, such that its error is minimum for the given input vectors and target vectors. In other cases the numeric problems prohibit direct calculation. Fortunately, we can always train the network to have a minimum error using the Widrow-Hoff learning rule.

With this we can design an adaptive linear system that responds to changes in its environment as it is operating. The linear networks which are adjusted at each time step based on new input and target vectors can find weights and appropriate bias which minimize the network and the sum squared error for recent input and target vectors. The networks of this type are often used in problems of error cancellation, signal processing and control systems.

Adaptive filtering is just one of the many more applications areas where the ADALINE has been used. To carry out this kind of application is necessary a new component to make complete use of the power of an adaptive network, this is a delay line. In figure 2 is shown the neuron pattern like adaptive filter that was used in this paper. The pattern has input signal from the left, and each one of them passes through  $N-1$  delays. The output of the tapped delay line (TDL) is an  $N$ -dimensional vector, made up of the input signal at the current time, the previous input signal, etc. These in turn pass through a linear activation function to obtain their output.

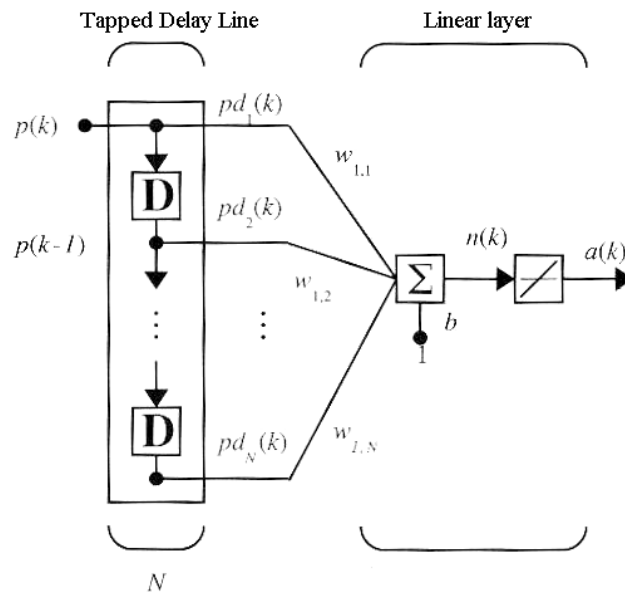


Figure 2. Neuron model like an adaptive filter

#### 4. PROCEDURE

When a failure occurs in a 16 elements linear adaptive array (LAA), the steering vector  $S$  is affected and therefore this damages the radiation pattern in the coefficients of the array factor ( $AF$ ). Then is supposed a zero in the fail element, with this a new radiation pattern is obtained for the  $M-1$  remaining array elements and the AANN adjusts the new parameters to adapt them to the original radiation pattern. Each radiation pattern is formed by 901 points that correspond to its amplitude and its phase for  $180^\circ$ , with a step of 0.2. For AANN to carry out its work, we made a preprocess of the original data, improving its functionality, moving all the points to positive values and then normalizing them in an interval of  $[-1,1]$ . To train the AANN we used the following code in MatLab:

First we read the data of a file, as much for the inputs as for the targets vectors:

```
'P = dlmread ('16e35db.dat','t',0,0,[0,0,901,0]);',
'T = dlmread ('16e35db.dat','t',0,1);',
```

Then the vectors are normalized in an interval of  $[-1,1]$ :

```
'[Pn,minp,maxp] = premmx(P);',
'[Tn,mint,maxt] = premmx(T);',
```

Thus they are linked and transpose (they make the data comfortable for the AANN)

```
'P = con2seq(Pn.);'  
'T = con2seq(Tn.);'
```

The linear network must have tapped delay in order to learn the time-shifted correlation between P (input vector) and T (target vector), NEWLIN creates a linear layer.',

```
'net = newlin([-1 1],1,[0 1],0.5);'
```

NEWLINE: has as parameters, ([-1 1] is the minimum value of input, 1 is the maximum value of the input (is the expected input range)], The second argument 1 is the number of neurons in the layer, [0 1] specifies one input with no delay and one input with a delay of 1, The last argument 0.5 is the learning rate);

```
'[net,Y,E,Pf]=adapt(net,P,T);'
```

ADAPT: simulates adaptive networks. It takes a network, an input signal, and a target signal, and filters the signal adaptively. By t=2 the network has learned the relationship between the input and the target and the error drops to near zero.

The process mentioned above repeats when there are two and three fails in the elements of LAA. The coefficients of the AF are presented for the remaining n-elements to generate the patterns with damage. These radiation patterns are shown in the figure 3, then the radiation patterns adjustment is presented together with the error for each array [8].

## 5. SIMULATIONS RESULTS

A 16-elements Linear Antennas Array (LAA) is used with Dolph-Tschebyscheff configuration, and separation of  $0.5[\lambda]$  (wavelength) with a non-uniform spacing, a Side Lobe Level (SLL) of -35 dB is used as a reference, and with the main beam pointing directed toward  $90^\circ$ .

The damage radiation patterns are obtained when one or more elements of ALA stop working by unforeseen reason, its correspond excitation coefficient in the array factor (AF) turns to zero. Then the adaptive artificial neural network (AANN) adjusts the parameters from these radiation patterns to the original parameters of 16-elements array. In figure 3 the radiation pattern is shown for 16 elements of LAA. The excitation coefficients of the AF for 16-elements are:

### *Excitation Coefficients for 16-elements LAA*

```
2.078  2.827  4.512  6.316  8.130  9.744  10.959  11.605  
11.605  10.959  9.744  8.130  6.316  4.512  2.827  2.078
```

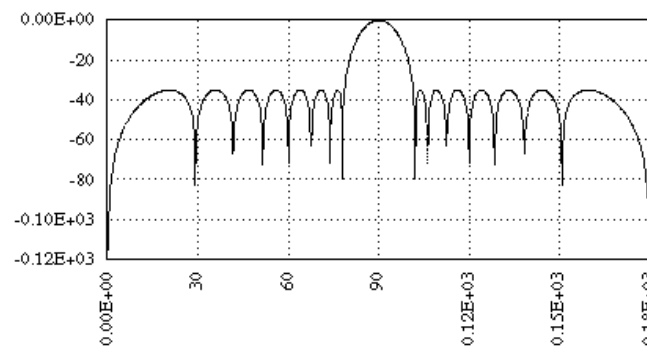


Figure 3. Radiation pattern for 16-elements of LAA

Characteristics of the output for 16-elements of the array:

DIRECTIVITY = 11.120 [dB]

DIRECTIVITY = 12.943 dimensionless

NUMBER OF MAXIMA BETWEEN 0 AND 180 DEGREES = 1

Half-Power Beam Width for maximum element =  $8.5^\circ$  for  $\theta_{MAX} = 90.0^\circ$

Following, when there is a failure in the second, fourth and sixth element of the linear antennas array the radiation patterns are shown.

*Failure of 1 - element*

*Excitation Coefficients for 16-elements LAA with 1 failure*  
 2.359 0.000 6.232 8.974 11.703 14.033 15.603 8.078  
 8.078 15.603 14.033 11.703 8.974 6.232 3.812 2.359

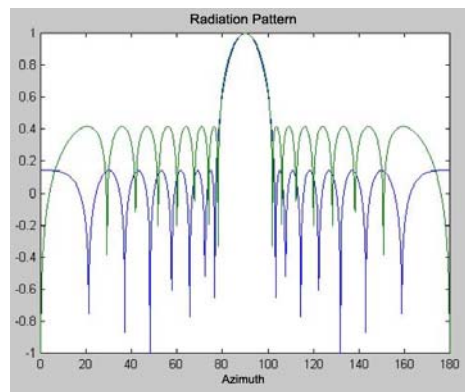


Figure 4. Radiation Pattern of 16-e (green) and radiation pattern with 1 failure (blue)

Characteristics of the output for 16-elements with 1 failure:

DIRECTIVITY = 10.730 [dB]

DIRECTIVITY= 11.830 dimensionless

NUMBER OF MAXIMA BETWEEN 0 AND 180 DEGREES = 1

Half-Power Beam Width for maximum element =  $9.3^\circ$  for  $\theta_{MAX} = 90.0^\circ$

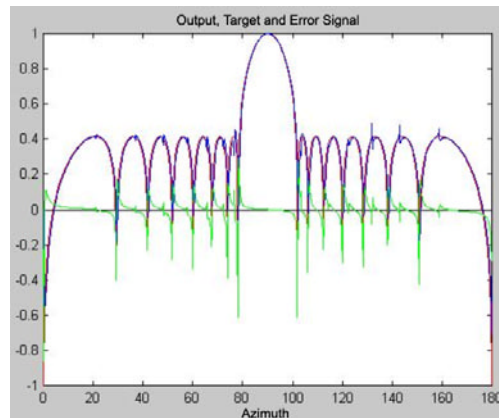


Figure 5. Radiation pattern of 16-e (red), radiation pattern with adjustment (blue) and error (green)

Failure of 2 – elements

Excitation Coefficients for 16-elements LAA with 2 failures  
 2.622 0.000 4.697 0.000 11.593 15.134 17.947 19.506  
 19.506 17.947 15.134 11.593 7.933 4.697 2.827 2.622

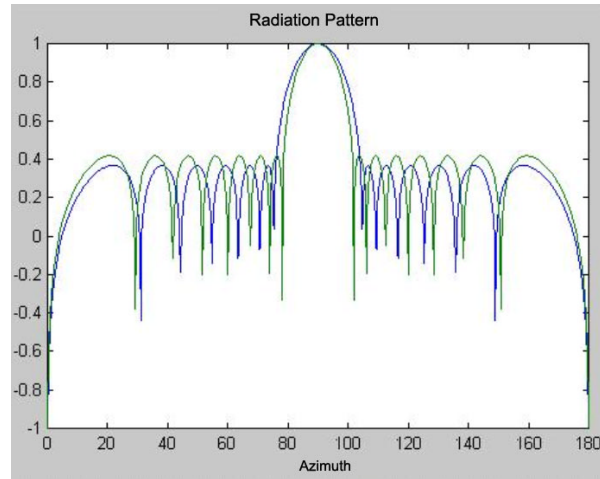


Figure 6. Radiation Pattern of 16-e (green) and radiation pattern with 2 failures (blue)

Characteristics of the output for 16-elements with 2 failures:

DIRECTIVITY = 10.374 [dB]

DIRECTIVITY = 10.898 dimensionless

NUMBER OF MAXIMA BETWEEN 0 AND 180 DEGREES = 1

Half-Power Beam Width for maximum element =  $10.1^\circ$  for  $\theta_{MAX} = 90.0^\circ$

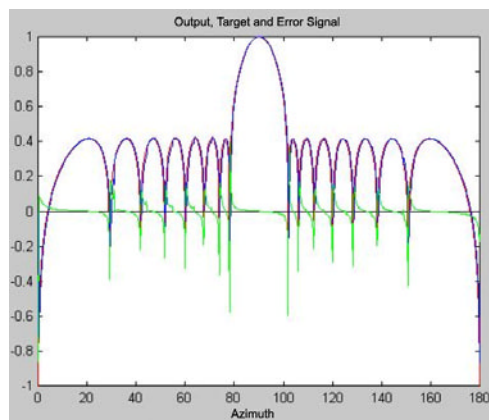


Figure 7. Radiation pattern of 16-e (red), radiation pattern with adjustment (blue) and error (green)

Failure of 3 – elements

Excitation Coefficients for 16-elements LAA with 3 failures  
 2.963 0.000 5.888 0.000 15.195 0.000 22.980 12.074  
 12.074 22.980 19.750 15.195 10.275 5.888 4.512 2.963

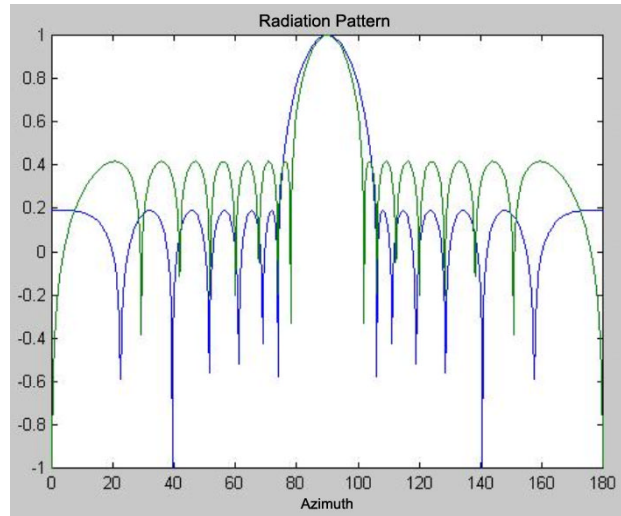


Figure 8. Radiation Pattern of 16-e (green) and radiation pattern with 3 failures (blue)

Characteristics of the output for 16-elements with 3 failures:

DIRECTIVITY = 9.997 [dB]

DIRECTIVITY = 9.994 dimensionless

NUMBER OF MAXIMA BETWEEN 0 AND 180 DEGREES = 1

Half-Power Beam Width for maximum elements =  $11^\circ$  for  $\theta_{MAX} = 90.0^\circ$

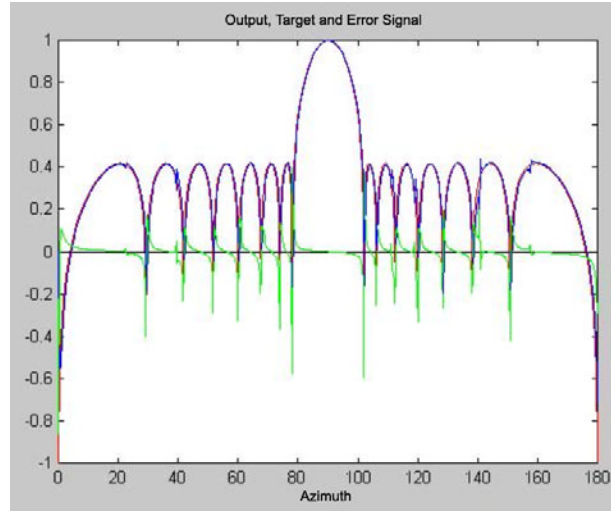


Figure 9. Radiation pattern of 16-e (red), radiation pattern with adjustment (blue) and error (green)

## 6. CONCLUSIONS

The radiation patterns correction that carries out the AANN (Adaptive Artificial Neural Network), when failures are presented in the linear array of antennas of 16-elements, are below 1% in the softest areas, and it is increased in the abrupt changes of the original radiation patterns. In some cases variations are presented in the adjustment (figure 5), but it is necessary to remember that during the training the learning rate of the AANN is very important in the adaptation of both patterns, the original and failure one.



The adjustment of the radiation patterns depends on excitation coefficients, because these coefficients support to generate the radiation pattern. However in the AANN the weights are parameters of correction which takes the damaged signal to the original, to reduce the level of the side lobes level (SLL). Thus the weights and biases of the network are the ones that adapt and correct the failures of damaged radiation pattern. These obtained AANN parameters are related with the excitation coefficients of the array and with the beamforming which yield the amplitude and the phase of the array.

The success correcting a damaged pattern depends strongly on the original weighting of the failed elements and of the number of failures in the array. In this instance, if in the linear antennas array (LAA) the eighth or ninth element fails resulting in a blockage, it would be impossible to correct or yield improvement using AANN or using any technique. We can observe that the failures occur on the same side with respect to the central element, but nevertheless could happen in both sides of the array also.

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