

# Reference Fields Analysis of a Markov Random Field Model to Improve Image Segmentation

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## ABSTRACT

In Markov random field (MRF) models, parameters such as internal and external reference fields are used. In this paper, the influence of these parameters in the segmentation quality is analyzed, and it is shown that, for image segmentation, a MRF model with a priori energy function defined by means of non-homogeneous internal and external field has better segmentation quality than a MRF model defined only by a homogeneous internal reference field. An analysis of the MRF models in terms of segmentation quality, computational time and tests of statistical significance is done. Significance tests showed that the segmentations obtained with MRF model defined by means of non-homogeneous reference fields are significant at levels of 85% and 75%.

Keywords: Image segmentation, unsupervised segmentation, Markov random field, non-homogeneous random field.

## RESUMEN

En modelos de Campos Aleatorios de Markov (MRF) se emplean parámetros como el campo de referencia interno y externo. En este artículo, analizamos su influencia en la calidad de la segmentación final, y mostramos que, para segmentación de imágenes, un modelo MRF con una función de energía definida mediante un campo de referencia interno y uno externo no homogéneos, obtiene mejores calidades de segmentación que un modelo MRF definido a través de un solo campo de referencia interno homogéneo. El análisis de los modelos MRF es realizado en términos de la calidad de segmentación, tiempo computacional y pruebas de significancia estadística. Las pruebas de significancia mostraron que los resultados de segmentación obtenidos con el modelo MRF definido a través de campos de referencia no homogéneos son significativos en un nivel del 85% y 75%.

## 1. Introduction

Image segmentation is a low-level image processing task that aims at partitioning an image into homogeneous regions [1]. With exception of trivial cases, segmentation is not a simple task because the homogeneity concept in regions is difficult to threat in automatic processes. In real images, the objects that can be segmented easily by a human could be erroneously segmented and partitioned in a great amount of small regions by an automatic process.

Image segmentation is important because many high level processing tasks make use of a segmented image, for examples: satellite image classification in remote sensing applications, image understanding and interpretation, object

recognition and surface description. In all these tasks, the segmentation results affect severely the results of subsequent processes.

Markov random field [2] is a probabilistic model that has been successfully applied to problems of image segmentation [3, 4]. MRF models provide a convenient way of modeling spatial contextual information among neighboring pixels. MRF models in computer vision for image segmentation are formulated within the Bayesian framework. The optimal solution of a segmentation problem is defined as the maximum a posteriori (MAP) probability estimate, and it is computed minimizing the posterior energy  $p(x|y)$ . This energy depends on a data likelihood model  $p(y|x)$  and a priori model  $p(x)$  in which contextual constraints are defined. The practical use of MRF models is largely

ascribed to the equivalence between MRF and Gibbs probability distributions [2, 5].

A MRF model called TS-MRF (tree-structured Markov random field) [6, 7, 8] has been recently used for segmentation [7, 8, 9, 10]. TS-MRF is a recursive model with a fast optimization, capable to split highly correlated classes. The differences between TS-MRF model and a FLAT MRF model are 1) TS-MRF uses a binary tree structure to carry out the segmentation and 2) in each tree node a binary FLAT MRF is estimated along with all its associated parameters [6]. In the literature on MRF model based image segmentation [3, 4, 7, 8, 9, 10, 11, 12, 13, 14], the Gibbs energy is defined by an auto-model [5], which is a second-order energy function that involves up to pair-site cliques. In this energy only pair-site cliques and a homogeneous internal reference field are used. In [15, 16] a Texture Energy Function (TEF) for MRF models used for image segmentation is presented. The TEF consists of a likelihood model with Gaussian distribution  $p(y|x)$  and a second-order energy function with non-homogeneous internal and external fields obtained by means of the 2-D Wold decomposition [17]. Unlike models in literature, where homogeneity is assumed for mathematical and computational convenience, in this function both fields are considered as non-homogeneous. In this paper, we analyze the importance of non-homogeneous reference field parameters, as in

function TEF, to obtain better image segmentation quality. The analysis is done in terms of segmentation quality, tests of statistical significance and computational time. Significance tests showed that segmentations obtained with the MRF model defined by means of non-homogeneous reference fields are significant at levels of 85% and 75%.

## 2. Texture Energy Function

References [15, 16] define a prior energy function by means of a non-homogeneous auto-model. The a priori energy function, or Gibbs energy, consists of a second-order energy function with clique potentials defined from texture fields obtained by means of the 2-D Wold decomposition [17]. In 2-D Wold decomposition, the texture image is assumed to be a realization of a 2-D homogeneous random field, and based on Wold decomposition, the texture image is decomposed into a sum of two texture fields: a structural texture field  $V$  and a stochastic texture field  $W$ .

Therefore, the external field of a priori energy function  $\alpha_s$  is defined by means of a structural texture field  $V$  and internal field of a priori energy function  $\beta_{sr}$  is defined by means of a stochastic texture field  $W$ .

Let  $\beta_{sr}$  be a function defined as follows:

$$V_2(x) = \begin{cases} \beta^{sr} = |w_s - w_r| & \text{if } s \neq r \text{ and } s, r \in C_2 \text{ and } w_s, w_r \in W \\ 0 & \text{otherwise} \end{cases} \quad (1)$$

where  $C_2$  is the set of pair-site cliques of second order,  $w_s$  and  $w_r$  are the gray values at sites  $s$  and  $r$  for pixels in  $W$ .

Based on this, the a priori energy is defined by means of reference texture fields  $V$  and  $W$  as:

$$U(x) = \sum_{s \in C_1} v_s x_s + \sum_{s, r \in C_2} \beta^{sr} x_s x_r \quad (2)$$

where  $x_s$  and  $x_r$  are values at sites  $s$  and  $r$  for pixels in  $X$ ,  $\beta^{sr}$  is obtained by (1),  $v_s \in V$  and  $C_1$  is the set of single-site cliques. On the other hand, the likelihood model is defined as in [7], and finally, the posterior texture energy function TEF is defined as

$$x_{MAP} = \underset{s \in S}{\operatorname{argmin}} \left[ \ln 2\pi^2 |Cov_k|^{1/2} + \frac{1}{2} (y_s - \mu_k)^T + (Cov_k)^{-1} (y_s - \mu_k) \right. \\ \left. + \ln Z + \frac{1}{Z} \left[ \sum_{s \in C_1} v_s x_s + \sum_{s,r \in C_2} \beta^{sr} x_s x_r \right] \right] \quad (3)$$

where  $\mu_k$  and  $Cov_k$  are the mean and the covariance matrices of class  $k$  respectively,  $y_s$  is the gray value in the site  $s$ ,  $B$  is the band number in the image and  $Z$  is the partition function. The TEF is integrated within a TS-MRF model and, contrary to models in the literature and to TS-MRF original model, this posterior energy uses both reference fields different from zero ( $v_s = \alpha_s \neq 0$ ,  $\beta^{sr} \neq 0$ ) and allows non-homogeneous sites.

### 3. Analysis of reference fields to improve image segmentation

We carried out experiments to analyze the influence of parameters such as internal and external reference fields in segmentation quality. Particularly, the performance of the Texture Energy Function (TEF) proposed in [15, 16] is evaluated. The TEF uses an a priori energy function with non-homogeneous internal and

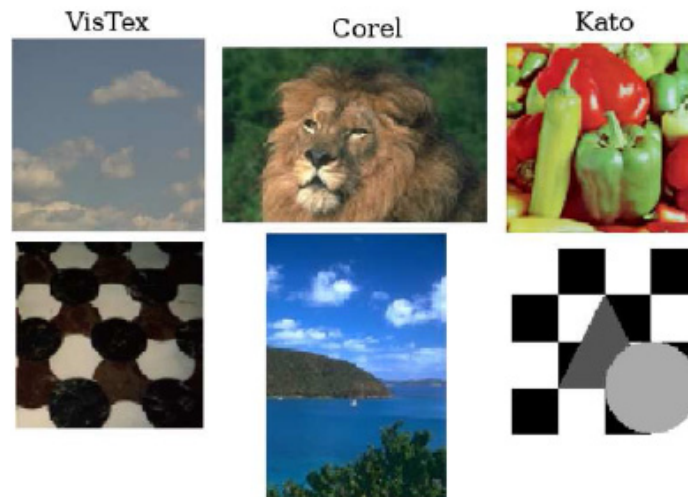


Figure 1. Examples of real and synthetic images.

external fields obtained by means of the 2-D Wold decomposition [17]. The structural component is defined to be the external field of a priori energy function  $\alpha_s$  and the stochastic component is defined to be the internal field of a priori energy function  $\beta^{sr}$  (Eq. 1 and 2). The function TEF is integrated within an unsupervised flat MRF model (MRF-FUS), and an unsupervised tree-structured Markov random field model (TS-MRF) in order to evaluate its performance. The function TEF is tested on a variety of synthetic and real images. Real images have been obtained from MIT's VisTex [18] and Corel [19] databases. Real images are segmented manually to obtain the segmentation map and quality is obtained evaluating the percentage of mis-segmented pixels. The synthetic images have been obtained from [20] and synthetic noise is added. Noisy synthetic images were produced by adding 3 kinds of common radiometric noise on remote sensing images [21, 22]: 1) striping (different over all brightness of adjacent lines), 2) drop line (null scan line) and 3) noise (dark and bright points at the background). The first noise is simulated by randomly selecting three lines and setting pixel values to white (255). The second noise is simulated by randomly selecting three lines and setting pixel values to black (0). Finally, the third noise is simulated by adding 0 mean Gaussian noise to the original synthetic image.

Examples of real and synthetic images are shown in Figure 1.

### 3.1 Sensitivity of reference fields in the segmentation quality

First, experiments on synthetic images were carried out in order to analyze how the values of internal and external reference fields are sensitive to initialization. Figure 2 shows how the segmentation quality is influenced by the reference fields  $\beta$  and/or  $\alpha$ . The plot in Figure 2 (—○—) represents segmentation accuracy for the case of a flat MRF model, defined by means of an energy function with an homogeneous internal reference field ( $\alpha=0$  and  $\beta \neq 0$ ), whereas the plot in Figure 2 (—●—) represents accuracy for the case of a flat MRF model defined by means of an energy function with homogeneous internal and external fields ( $\alpha \neq 0$  and  $\beta \neq 0$ ). We can see that a slightly change of initial values of  $\alpha$  and  $\beta$  may cause that final segmentation accuracy changes. In domains where segmentation depends on very similar object attributes, the problem complexity increases [15, 23] and becomes desirable to increase segmentation accuracy in few pixels because on studies on land cover segmentation in remote sensing applications, the final amount of mis-segmented pixels involves  $km^2$  of surface when they are corresponded to the ground. In these

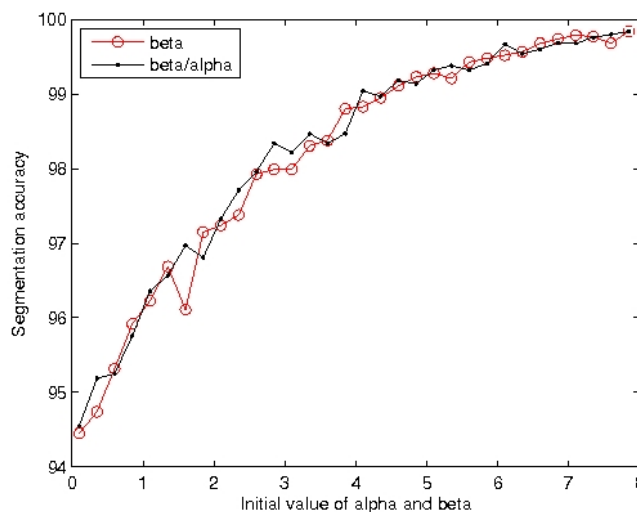


Figure 2. Plot of segmentation accuracy using different values of alpha and beta.

experiments, we can see from Figure 2 that using an a priori energy function with internal and external fields helps to obtain better accuracy that by using an energy function with only an internal reference field. For example, if we considered  $\alpha=0.5$  and  $\beta=0.5$ , a 95.2% of segmentation accuracy is reached whereas with only  $\beta=0.5$ , the percentage falls to 94%. Another example can be seen with  $\alpha=1.75$  and  $\beta=1.75$  where a 97% segmentation accuracy is reached and a 96% with only  $\beta=1.75$ .

### 3.2 Tests of segmentation accuracy

The application was developed in MATLAB 7.1 to obtain the Wold decomposition and the segmentation using MRF models. The application software has been executed in a computer with an Intel Centrino processor at 1.66GHz, 1GB RAM in memory and a Linux operating system. To carry out segmentation using the function TEF and any MRF model, first it is necessary to estimate the texture reference fields  $V$  and  $W$  using Wold

decomposition. The Wold algorithm used in the implementation can be found in [24]. The parameters of cut frequency  $f_c$ , evanescent line number  $L_e$ , edge filter and edge threshold  $threshold_e$ , necessary for the decomposition, were manually selected and fitted to each image. An example to obtain the harmonic component of Wold decomposition can be seen in Figure 3 using a cut frequency  $f_c=11.5$ . Figure 4 shows an example to obtain the evanescent component of the same image using 2 evanescent lines  $L_e$ ; the edge filter used was Canny and edge threshold  $threshold_e=0.03$ . The structural component  $W$  is estimated by summing the harmonic and evanescent component as shown in Figure 5. Finally, the stochastic component is obtained by the remaining image (see Figure 6).

Once the Wold decomposition has been carried out, the segmentation can be obtained using the function TEF and the TS-MRF model (see Figure 7).

The Correct Segmentation Accuracy (CSA) is estimated using Equation (4).

$$CSA = \frac{\text{Total number of correct segmented pixels}}{\text{Total number of pixels at the image}} \quad (4)$$

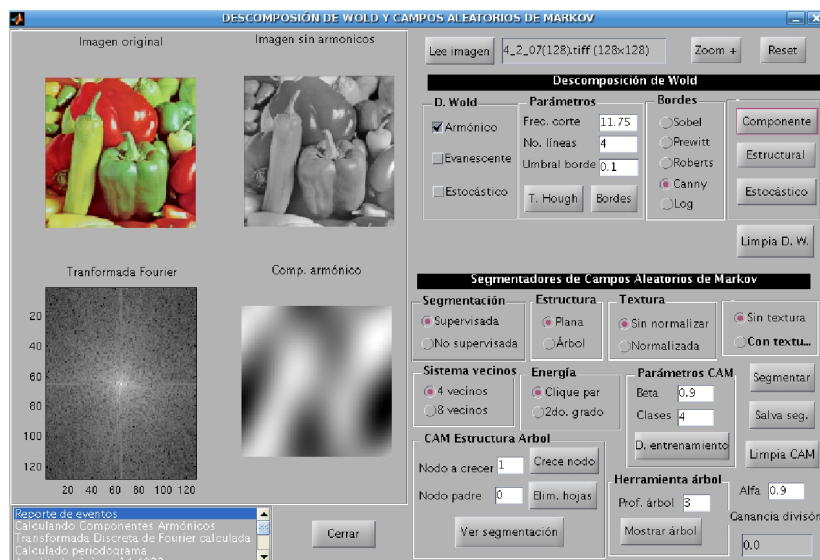


Figure 3. Obtaining harmonic component.

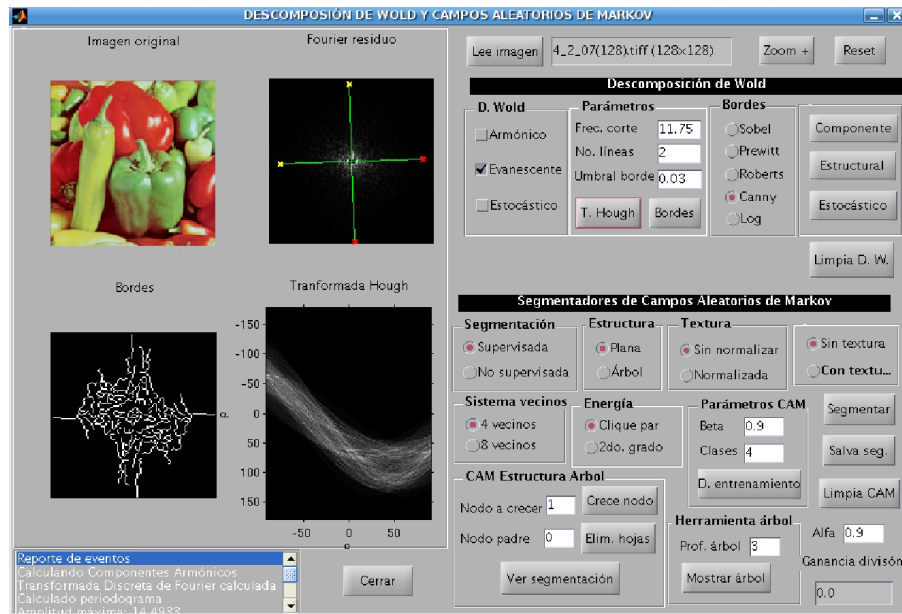


Figure 4. Obtaining evanescent component.

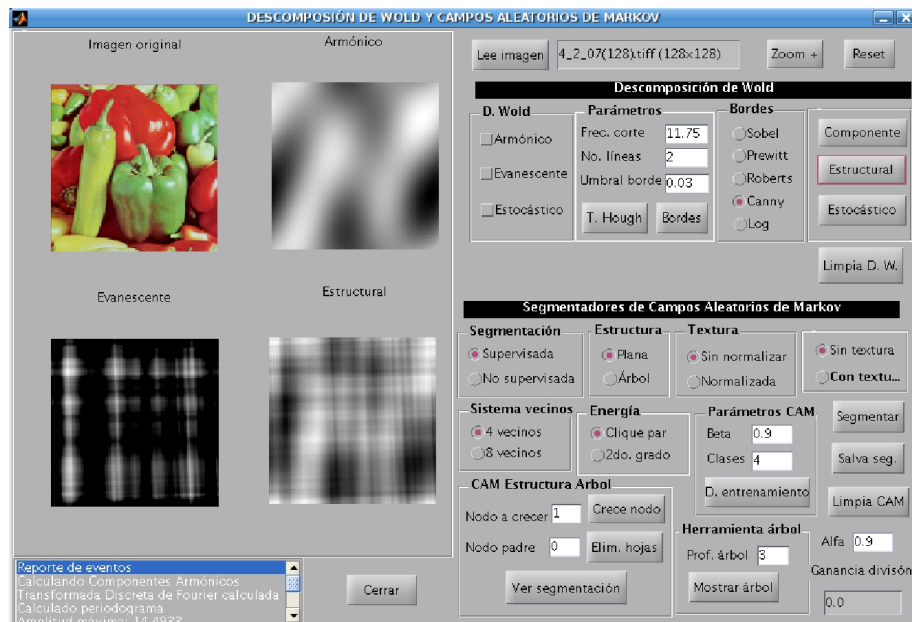


Figure 5. Obtaining structural component W.

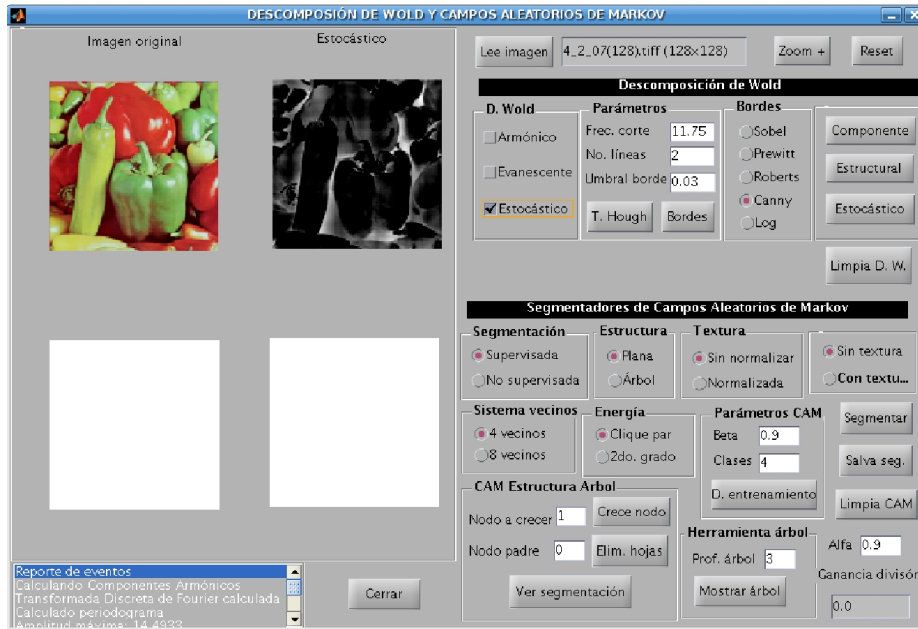


Figure 6. Obtaining stochastic component V.

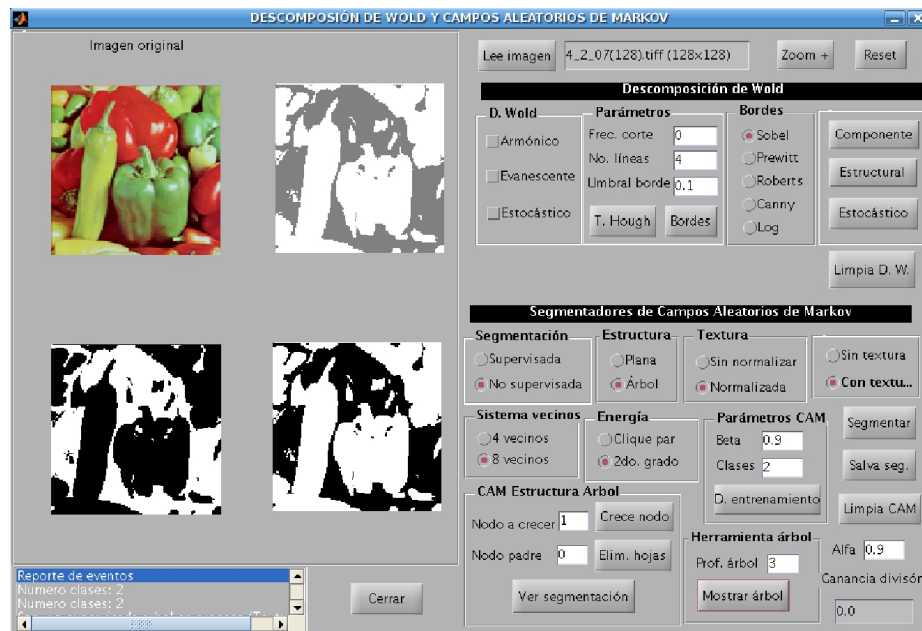


Figure 7 Segmentation using TS-MRF/TEF.

The correct segmentation accuracy obtained with Equation (4) for synthetic images using MRF models is presented in Tables 1 and 2. We can see that, for the TS-MRF/TEF model, the correct segmentation accuracy decreases as the image is contaminated by a greater amount of noise. Something similar happens with the TS-MRF original model. In the six experiments, the TS-MRF/TEF model obtained the best results.

Figure 8 shows a visual comparison between the segmentation obtained with MRF-FUS and the segmentation obtained with TS-MRF/TEF. In this image, 2 classes were defined: airplanes and sky. We can see that the image is better segmented using the TS-MRF/TEF model.

Figure 9 shows a visual comparison for two images between the segmentation obtained with MRF-FUS, MRF-FUS/TEF and TS-MRF/TEF. The segmentation is improved, when the function TEF is introduced to an MRF-FUS model (see examples in Figure 9a and 9b). Figure

9c shows how a FLAT segmentation with function TEF is improved when both an MRF model not FLAT (i.e. a model based in a binary tree structure) and the function TEF are introduced.

Figure 10 shows a visual comparison for a remote sensing image. In this case, segmentations obtained with TS-MRF (Figure 10a) and TS-MRF/TEF models (Figure 10b) are compared. Table 3 shows other correct segmentation accuracies for real images. We can see that the segmentation accuracy is improved when the function TEF is introduced.

<i>Image</i>	<i>TS-MRF</i>	<i>TS-MRF/TEF</i>
13dB	91.64	<b>92.02</b>
5dB	59.2	<b>74.44</b>
3dB	64.19	<b>64.29</b>

Table 1. Segmentation accuracy using TS-MRF and TS-MRF/TEF models for Gaussian noise.

<i>Image</i>	<i>TS-MRF</i>	<i>TS-MRF/TEF</i>
13dB + Striping + Drop line	<b>89.32</b>	89
5dB + Striping + Drop line	65.7	<b>65.82</b>
3dB + Striping + Drop line	59.39	<b>59.51</b>

Table 2. Segmentation accuracy using TS-MRF and TS-MRF/TEF models for Striping, Drop line and Gaussian noise.



Figure 8. Segmentation using a) MRF-FUS, b) TS-MRF/TEF and c) original image.



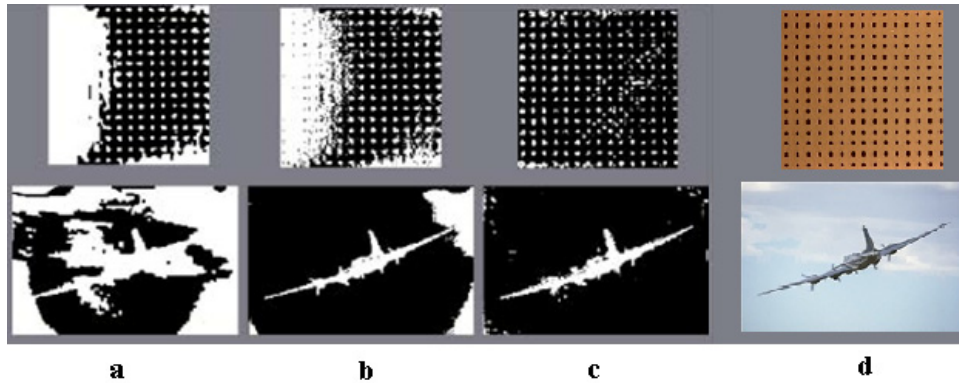


Figure 9. Segmentation using a) MRF-FUS, b) MRF-FUS/TEF, c) TS-MRF/TEF and d) original image.

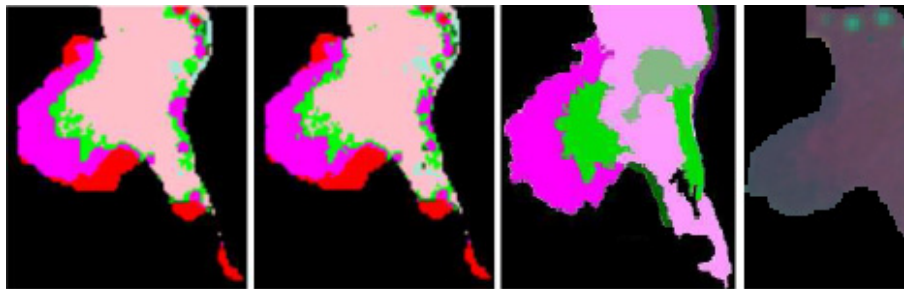


Figure 10. Segmentation using a) TS-MRF, b) TS-MRF/TEF, c) real segmentation obtained by means of field studies and d) original image.

<i>Image</i>	<i>MRF-FUS</i>	<i>TS-MRF</i>	<i>TS-MRF/TEF</i>
Image 6	52.43	64.51	<b>64.74</b>
Image 8	87.91	<b>93.73</b>	93.51
Remote sensing image	--	57.05	<b>58.39</b>

Table 3. Segmentation accuracy using MRF-FUS, TS-MRF and TS-MRF/TEF models for real images.

### 3.3 Tests of statistical significance

In order to find the significance level of the results, first the MRF-FUS model is compared against the TS-MRF/TEF model. Afterwards, we compared the original model TS-MRF against the TS-MRF/TEF model. To estimate the significance level of different observations in each sample with homogeneous variance, the following equation was used:

$$t = \frac{X_A - X_B}{\sqrt{\frac{\gamma_{AB}^2}{NA} + \frac{\gamma_{AB}^2}{NB}}} \quad (5)$$

where  $X_A$  and  $X_B$  denote the average of samples  $A$  and  $B$  respectively,  $NA$  and  $NB$  are the number of observations in  $A$  and  $B$ , respectively, and  $\gamma_{AB}^2$  is the variance of  $AB$  defined as

$$\gamma_{AB}^2 = \frac{(NA - 1)\gamma_A^2 + (NB - 1)\gamma_B^2}{(NA - 1) + (NB - 1)} \quad (6)$$

where  $\gamma_A^2$  and  $\gamma_B^2$  are the variances of samples  $A$  and  $B$ , respectively.

First, the significance level for MRF-FUS and TS-MRF/TEF models is obtained. Taking into account the segmentation accuracy of the previous section, and considering the TS-MRF/TEF model as sample  $A$  and the MRF-FUS model as sample  $B$ , we obtained the statistics for each sample (see Table 4). In order to evaluate homogeneity of variances, we divided the largest variance (sample  $B$ ) by the smallest variance (sample  $A$ ) to give an  $F$ -ratio. In this case a value of 1.11 is computed. Now, searching in an  $F$ -Table using the numerator degrees of freedom ( $NB-1$ ), and the denominator degrees of freedom ( $NA-1$ ), a value of 3.074 is found. Because the computed value is less than the tabled value, we can assume homogeneity of variances. Using Equation 4 in this experiment, a value of 1.21018 is computed. Searching in a  $t$ -table with  $(NA - 1) + (NB - 1)$  degrees of freedom, a value of 1.0880 is obtained at a significance level of 85%. We can see that this value is less than the

tabled value  $t$ ; therefore, we can assume that the segmentation differences were statistically significant.

	Sample A	Sample B
N	8	4
$\sum x_i$	679.85	289.47
Average X	84.9812	72.3675
$\sum x_i^2$	59388.7655	21716.9215
$\gamma^2$	230.609	256.2338
Standard deviation	15.1858	16.0073

Table 4. Statistics for TS-MRF/TEF and MRF-FUS models.

On the other hand, in Table 5, statistics to obtain the significance level between TS-MRF and TS-MRF/TEF models are shown. In this test, the TS-MRF model is considered as sample  $A$  and the TS-MRF/TEF model is considered as sample  $B$ . The computed value  $F$  is 1.15, searching in the  $F$ -Table using as numerator 10 degrees of freedom, and as denominator 13 degrees of freedom, we found a value of 2.138. Because the computed value is less than the tabled value, we can assume homogeneity of variances. Using Equation 4, a value of 0.79104 is computed. Searching in a  $t$ -Table with 23 degrees of freedom, a value of 0.6853 is obtained at a significance level of 75%. This value is less than the tabled value  $t$ ; therefore, we can assume that the segmentation differences were statistically significant

	Sample A	Sample B
N	11	14
$\sum x_i$	830.01	1125.37
Average X	75.4555	80.3836
$\sum x_i^2$	65210.6731	93378.2385
$\gamma^2$	258.1891	224.383
Standard deviation	16.0683	14.9794

Table 5: Statistics for TS-MRF/TEF and TS-MRF models.

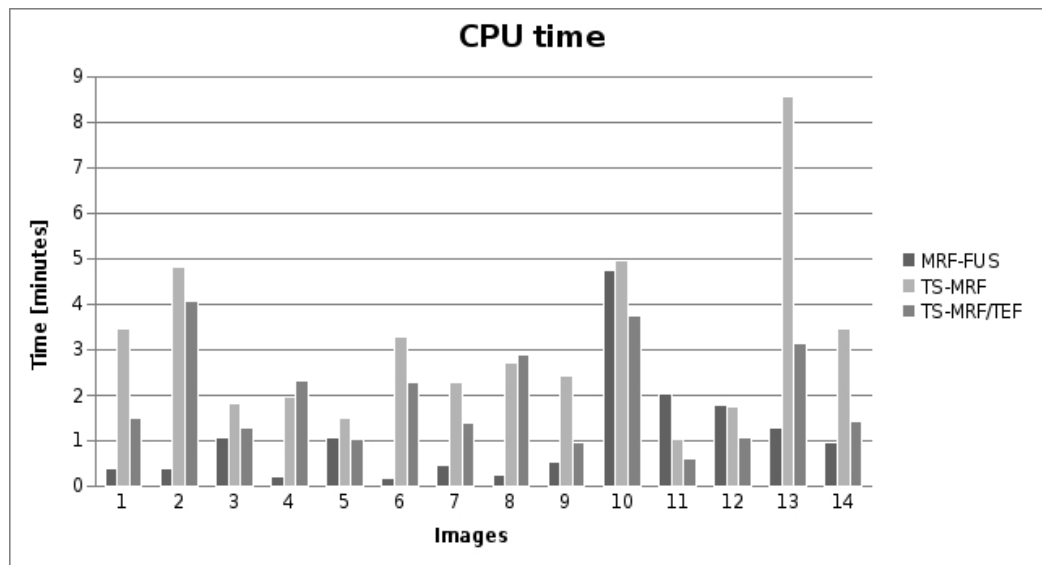


Figure 11. CPU time.

### 3.4 Computational time analysis

Figure 11 shows the CPU time for some test images. In general, the CPU time for the MRF-FUS model is less than the CPU time for the TS-MRF and TS-MRF/TEF models due to the fact that in these models the reference field parameter estimations are not done, and the internal reference field  $\beta$  is set to 0.9 because this value has been found to provide satisfactory results in the experiments. On the other hand, the CPU time for the TS-MRF/TEF model is less than the CPU time for the TS-MRF model in 12 of 14 segmentations. In both models, parameter estimations are done. TS-MRF uses PML (Pseudo-likelihood) [2, 25] whereas TS-MRF/TEF uses Wold decomposition [17]. The non-homogeneity of reference fields did not affect the CPU time of the model. Average CPU time for segmentations using an MRF-FUS model is one minute, for the TS-MRF/TEF model is two minutes and for the TS-MRF is three minutes.

### 4. Conclusion

This paper has analyzed the influence of parameters as internal and external reference fields of MRF models in the segmentation quality. Experiments are done on synthetic images to show that an a priori energy function with internal and external fields, as in texture energy function TEF, helps to obtain better segmentation accuracy than an energy function with only an internal reference field. Experiments with synthetic and real images show that the model that uses the function TEF (TS-MRF/TEF) improves the segmentation quality, and statistical significance tests showed that the segmentations obtained with this model are significant at the 85% level in comparison with a flat MRF model, and are significant at the 75% level in comparison with a TS-MRF model. In conclusion, we can say that differences between the obtained segmentations are caused by the introduction of the function TEF. In addition, the CPU time for TS-MRF/TEF model is comparable with the CPU time for TS-MRF.

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