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Original

New modified Bat algorithm for blind speech enhancement in time domain

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Abstract: We address the speech enhancement problem for dual convolutif mixed channel by viewing it in a blind separation source setting. One widely used technique to separate mixed signals is to apply adaptive filtering, the challenge is to identify an unknown finite impulse response. Traditionally we apply a gradient-based algorithm to adapt filter coefficients. However, such algorithms often suffer from premature convergence when using large filters and non-stationary inputs leading to the socalled local minimum problem, which affects the quality of enhanced signals significatively. One alternative to overcome this problem is to apply a population-based metaheuristic algorithms in which filter coefficients are adapted iteratively by minimizing a cost function. But even with this metaheuristic-based solution, local minimum problem at large filters still exist. To avoid local minima and improve the chance to reach the global solution. We propose in this paper, a novel algorithm called a modified Bat algorithm to render the search process efficiently by enhancing its capability of exploration and exploitation. Several experiments under different noise types are conducted using our proposed modified Bat algorithm in comparison with some of the popular state-of-the-art algorithms. The enhanced signals obtained by each algorithm at the separation process outputs show good behavior and superiority of our proposed algorithm. In terms of system misalignment, as well as a segmental signal-to-noise ratio.

Keywords: Speech enhancement, blind source separation, population-based metaheuristic algorithms, system misalignment, segmental signal-to-noise ratio

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1. Introduction

Adaptive noise cancellation (ANC) is an alternative approach used to improve the quality of corrupted speech signal by different noises (Loizou, 2013). Numerous techniques were suggested to enhance the speech signal using the gradientbased algorithm family (Widrow et al., 1975). The most used algorithms from this family are the least mean square (LMS) and normalized least mean square (NLMS) algorithms (Rogers, 1996). However, gradient-based algorithms suffer from the local minimum optimization problem and the global solution is seldom attained. To avoid local minimum solutions in the ANC, many modifications of the normalized least mean square were proposed such as variable step size NLMS (VSS-NLMS) (Bendoumia & Djendi, 2015), and the wavelet-domain NLMS algorithms (Djendi, 2018).

In order to overcome this problem, algorithms-based metaheuristic algorithms are advised due to their simple implementation. Furthermore, metaheuristics are well known for their ability to avoid premature convergence and lead to a lowest chance of falling in local minima (Mahbub et al., 2010). Various metaheuristic algorithms have been used to resolve the ANC problem using adaptive infinite impulse response filters (IIR). The authors Chang and Chen, (2010), Kunche (2016) suggested to use a Bat algorithm (BA), genetic algorithm (GA), particle swarm optimization and its variant version to be applied in ANC.

The aim of this paper is to propose a new efficient modified Bat algorithm which will be implemented in a blind speech enhancement structure (in this work, we only consider the convolutive mixture of signals (Djendi, 2010)) . Note that this paper is an extended version of our work published in Fisli et al. (2019). we extend the previous version by a new theoretical basis and some efficient modification which will increase its performance and therefore the possibility to apply it in other scenarios involving other types of noise. The remains of this manuscript are organized as follows, in the second section, we review the mixing process that produces mixed signals, then the forward blind source separation structure (FBSS) is presented, in Section 3 standard BA is reviewed. Then our modified version of BA is presented. Simulation results discussions are discussed in Section 4. Finally, the paper is concluded.

2. Problem formulation

2.1. Mixture model

In Figure 1, we show the scheme of the convolutive mixture model (two source signals recorded by two microphones), where $s_1(k)$ denote the speech signal, $s_2(k)$ represent the punctual noise (Djendi, 2010).

 $m_1(k)$ and $m_2(k)$ is the mixing process output, these two outputs are given by:

$$m_1(k) = s_1(k) * h_{11}(k) + s_2(k) * h_{21}(k)$$
(1)

$$m_2(k) = s_2(k) * h_{22}(k) + s_1(k) * h_{12}(k)$$
(2)

where $h_{11}(n)$ and $h_{22}(n)$ represent direct channel paths, $h_{12}(k)$ and $h_{21}(k)$ represent the cross-coupling effects between the channels, all these impulse responses are a finite impulse response (FIR), however, the symbol (*) denote the convolution operator.

A complete mixing process can be simplified by considering some assumption:

• Original signals are a clean speech and a noise signal, i.e., $s_1(k) = s(k)$, $s_2(k) = b(k)$.

• Direct channel paths are considered equivalent to the unit impulse response, i.e.

$$h_{11}(k) = h_{22}(k) = \delta(k)$$
.

• Moreover, we assume that input signals are statistically independent.

• Note that simplified convolutive mixing is widely used because it is well approved in theory and practice.



Figure 1. The convolutive mixture model.

Figure 2 shows the new simplified convolutive model where the two noisy signals at each channel can be written as:

$$m_1(k) = s(k) + b(k) * h_{21}(k)$$
 (3)

$$m_2(k) = b(k) + s(k) * h_{12}(k)$$
(4)



Figure 2. The simplified convolutive mixture model.

2.2. Forward blind source separation structure

In Figure 2, we suppose that we have no prior knowledge about the two input signals s(n), b(n) and the two cross-coupling impulse responses $h_{12}(n)$ and $h_{21}(n)$. In this

(8)

situation, we call the technique that estimates the original signals by using only the observation, the blind source separation (BSS). In this technique two structures are applied to retrieve the original signals (Bendoumia & Djendi, 2015).

Forward and backward structures are frequently used in BSS due to their efficiency involving speech enhancement for hearing aids, speech recognition and teleconferencing systems. In this work we used forward blind source separation structure (FBSS), (see Figure 3). Note that FBSS can be used only when all observed signal of the separation process is a simple linear combination of the input signals. Outputs available at the FBSS structure are:

$$Out_1(k) = p_1(k) - p_2(k) * w_{21}(k)$$
(5)

$$Out_2(k) = p_2(k) - p_1(k) * w_{12}(k)$$
(6)

inserting (1) and (2) into (3) and (4), respectively, we get:

$$Out_1(k) = b(k) * [h_{21}(k) - w_{21}(k)] + s(k) * [\delta(k) - h_{12}(k) * w_{21}(k)]$$
(7)

 $Out_2(k) = s(k) * [h_{12}(k) - w_{12}(k)] + b(k) * [\delta(k) - \omega_{12}(k)] + b(k) * [\delta(k)$

 $h_{21}(k) * w_{12}(k)$]



Figure 3. The FBSS structure model.

to obtain the optimal solution of the FBSS, we assume that $: w_{12}(n) = h_{12}(n)$ and $w_{21}(n) = h_{21}(n)$ thus the output equation of the unmixed signals is given by:

$$Out_1(k) = s(k) * [\delta(k) - h_{12}(k) * w_{21}(k)]$$
(9)

$$Out_{2}(k) = b(k) * [\delta(k) - h_{21}(k) * w_{12}(k)]$$
(10)

from (9) and (10), we can get the two-input signal estimation at the output, $Out_1(k)$ and $Out_2(k)$ with spectral and temporal distortions. Consequently the use of post-filters at output may be necessary (Djendi et al., 2006).

In this work, we consider only the case when the two microphones are lightly spaced, which leads to a low distortion, therefore, $\hat{s}(k) = Out_1(k)$ and $\hat{b}(k) = Out_2(k)$. To obtain the estimated source signals yield to obtain an

optimal solution for the adaptive filter, $w_{12}(k)$ and $w_{21}(k)$, which we can obtained by minimizing the following objective function:

$$J = \frac{1}{L} \sum_{k=0}^{L} Out_i(k)^2$$
 (11)

where *L* is the input frame length and i = 1, 2 is the channel index.

2.3. Framework for adaptive filtering in FBSS based on metaheuristic

In general, to solve optimization problems with a metaheuristic algorithm, one needs to evaluate the cost functions at each iteration using a set of input data. In FBSS problems, the mixed signals which represent the input signals of the online adaptive filter are not entirely available, therefore, the efficient way to proceed is to evaluate the cost function using the available frame of observed signal at each iteration. Moreover, we propose, in this paper, to use a manual voice activity detection (MVAD) system to control the adjustment of the adaptive filter, therefore the manual adaptation control, allow to evaluate the cost function only during the noise presence period in the case of the filter $w_{21}(k)$, whereas the filter $w_{12}(k)$ is updated during the voice activity presence periods. The general scheme of the proposed dual adaptive filtering by FBSS and metaheuristic algorithm is illustrated in Figure 4.

3. Algorithms review

Bat algorithms and modifications made to improve its efficiency are presented in this section.

3.1. Bat algorithm (BA)

The Bat algorithm (BA) belongs population-based algorithm (Yang, 2010). The bat can hunt even in the whole darkness using the echo return; this characteristic allows bats to differentiate between obstacles and insects as shown in Figure 5. The mechanism of echolocation can be modeled using a set of mathematical equations that consists of a bat swarm representing a potential solution, each bats move according to its velocity v_i and position x_i in land space according to a frequency f_{min} , variable wavelength γ and loudness A_0 to search for prey location. Bats fine-tune the emitted pulse frequencies and the pulse emission rate, using the distance between them and prey. Optimization process is then repeated until the maximum number of iterations is reached; the position and velocity are updated using the following relations: of iterations is

$$f_i = f_{min} + (f_{max} - f_{min}) \delta_b \tag{12}$$



Figure 4. Flowchart of the proposed dual adaptive FBSS -based metaheuristic algorithms.

$$\boldsymbol{v_i}^n = \boldsymbol{v_i}^{n-1} + (\boldsymbol{x_i}^n - \boldsymbol{g}^n) f_i$$
(13)

$$\boldsymbol{x_i}^k = \boldsymbol{x_i}^{k-1} + \boldsymbol{v_i}^k \tag{14}$$

were

 f_{min} , f_{max} : frequency min and max

 f_i : frequency of the $i^{
m th}$ bat,

 $\boldsymbol{v}_i^{n}, \boldsymbol{x}_i^{n}$: velocity and position of the i^{th} bat at time n,

 δ_b : a random vector distribution uniformly distributed,

G_{near}ⁿ : global near best solution,

however, a random walk is generated for each bat to improve the local search:

$$\boldsymbol{x_i}^n = \boldsymbol{x_i}^n + \varepsilon \boldsymbol{A_i}^n \tag{15}$$

were

arepsilon: random value in the range [-1, 1],

 A_i^n : loudness of the i^{th} bat at time n.



Figure 5. Bat echo location mechanism.

Furthermore, the loudness A_i and the rate r_i of pulse emission are updated a every iteration n. During the process the rate of pulse emission increases while the loudness decreases once a bat has found its prey, we use for simplicity $A_0 = 1$ and $A_{min} = 0$, which means that a bat has just met prey, therefore, bat stop to emit sound temporarily:

$$\boldsymbol{A_i}^{n+1} = \alpha \boldsymbol{A_i}^n \tag{16}$$

$$r_i^{n+1} = r_i^{0} (1 - e^{-\gamma t})$$
(17)

were α, γ : constant value, A_i^n loudness of the i^{th} bat at time n.

3.2. Formulation of the proposed modified Bat algorithm

Standard Bat algorithm has become very popular for solving real-world problem effectively, except in cases of higherdimensional problems where BA suffers from local minima problems, to overcome this handicap a modified Bat algorithm (MBA) is introduced to adapt the large adaptive filter. The decreasing nature of the acoustic filter requires to change the philosophy of generated the new solution by improving the local search. In our proposed MBA algorithm, we suggest updating loudness parameter A_i at each iteration which mean that loudness became variable during the optimization process by following a negative exponential function, loudness is estimated by:

$$A_i^n = \theta \ e^{-\mu(n-1)} \tag{18}$$

where

heta, μ : constants in the range of [0, 1],

moreover, by examination of real acoustic impulse responses, one can easily see the large distance between the

 ω :random value in te [-1, 1]

not the change is ignored.

pseudo-code.

this step is followed by evaluating the objective function,

The modified Bat algorithm is expressed by the following

the new solution is accepted unless it guarantees a lower

fitness value compared the one obtained by initial *Gbest*, if

first and the last point of impulse responses. In standard BA all the point filters are processed in the same way which prevents better exploitation and consequently lead to a wicked final solution. Wherefore in the proposed algorithm, we introduce another step to improve the quality of the solution by manipulating the elements of the best global solution individually according to the following equation:

 $Gbest(i) = Gbest(i) + \omega A_i^n$

(19)

c Begin

 \bullet Set problem dimension n ,number of Bat's, Maximum number of iterations maxit

the search space ${\it R}\,$, minimum and maximum

value of frequency f_{min} and f_{max} .

• Randomly generate positions X_i (i = 1, 2, ..., n) and velocity V_i (i = 1, 2, ..., n) of bat

• Define pulse frequency f_i

• Initialize pulse rates r_i and the loudness A_i

• Evaluate the objective function for each bat then to find the best initial fitness and the best global solution *Gbest*

While (t < maxit)

• Generate new solutions by adjusting frequency (Equation 12)

• Update frequency, velocities (Equations 13 and 14) If (rand > r_i) then

• Select a solution among the best solutions randomly.

• Generate a local solution around the selected best solution by a local random walk (Equation 15) End if

• Evaluate the objective function for each bat then and update the best fitness and Gbest

 $f(rand < A_i \& f(x_i) < f(Gbest))$ then

Accept the new solution Increases r_i using (Equation 17) and decrease A_i using the modified Equation (18) End if

• Evaluate the objective function for each bat then and update the best fitness and Gbest

For (j=1:n)

• Generate a new solution by manipulation only the j^{th} element of the Gbest (equation 19)

• Evaluate the objective function for the new Gbest

• Accept the change in the Gbest unless it guarantees a lower fitness value , if not the change is ignored

End For

End while

End

Return Gbest as the solution

4. Analysis of experimental results

In this section, we demonstrate the noise reduction capabilities of the proposed modified Bat algorithm in the context of speech enhancement. We perform extensive experiments under several different noisy observation and compare its performance to well-known metaheuristic algorithm including its original version Bat algorithm (BA), (Yang, 2010) particle swarm optimization (PSO) (Clerc, 2010) and gray wolf optimizer (GWO) (Okwu & Tartibu, 2021). We have used the simplified convolutive mixture model presented in Section 2. The clean speech signal s(k) is a sentence pronounced by one male speaker that is sampled at 8 kHz. We mixed clean speech using three different reel noise (k): white Gaussian, car, and USASI noises. The two impulse responses $h_{12}(k)$ and $h_{21}(k)$ are produced by random sequences, with exponentially negative functions (Djendi, 2010; Djendi et al., 2006). In Figure 6, we show a sample of the impulse response with length L=128, used to produce the mixing signals $m_1(k)$ and $m_2(k)$ where the input signals are a speech and USASI noise; the input SNRs at both sensors are $Snr_1 = Snr_2 =$ -6 dB (see Figure 7).

It should be mentioned that we have used all the instances described in Section 3 for all test, furthermore, the same population number, search space range and iteration numbers are used for all algorithms with the goal to evaluate the algorithm and then to get the better performance algorithm using the same setting. Moreover, results are conducted using three lengths of the adaptive filter L = 32, 64 and 128 and different input SNRs. Finally, all obtained results are averaged over 20 trial runs. Note that there are many manners to conduct the comparison of algorithm performances, in this work we propose to use two performance measures:

- System misalignment (SM) criterion that is defined as follows:

$$SM_{\rm dB} = 20 \log(\frac{\|h_{21} - w_{21}\|}{\|h_{21}\|}$$
(20)

where $\|.\|$ represent the Euclidian norm operator, $h_{21}(n)$ and $w_{21}(n)$ denote the real filter vector and the adaptive filter vector, respectively.

-Segmental signal-to-noise ratio (SegSNR) which is given by the following relation:

$$SegSnr_{dB} = 10log(\frac{\sum_{i=0}^{P-1} |s(i)|^2}{\sum_{i=0}^{P-1} |s(i) - Out_1(i)|^2})$$
(21)

where |.| represents the absolute operator, s(k) and $Out_1(k)$ are the original and the estimated speech signals respectively, P represents the number of samples needed to

obtain the average value of the output SNR. In all experiments we have used a manual voice activity detector (MVAD), which means that we update the filter $w_{21}(\mathbf{k})$ only in silence periods, whereas $w_{12}(\mathbf{k})$ is updated only in speech-periods (Djendi, 2010). We should mention that the noisy observations $m_1(\mathbf{k})$ and $m_2(\mathbf{k})$ are processed segment by segment with overlap technique where each segment involves 256 samples, segmentation is performed using Hamming window with 25% overlap between adjacent frames (Kunche, 2016).



Figure 6. A sample of impulse responses in left $h_{12}(k)$ and in right $h_{21}(k)$, with L = 128.



Figure 7. Original speech s(k) [top left], noise signal b(k) [top right], mixing signal $m_1(k)$ [bottom left], (mixing signal $m_2(k)$ [bottom right].

4.1. System misalignment (SM) evaluation

The experimental results in terms of SM criterion obtained by the four algorithms, i.e., BA (Bat algorithm), PSO (particle swarm optimization), GWO (gray wolf optimizer), and the proposed MBA algorithm are described in Figure 8 (we used the absolute value of each value to better illustrate the results). The parameters used to compute the output of each algorithm are summarized in Table 1. The adaptive filter length is variable, i.e., L=32, 64, and 128. The input SNRs are selected to be equal to -6 dB, 0 dB, and 6 dB. The punctual noise is white, USASI (United State of America Standard

Institute, now ANSI), and a car noise. Note that we are only interested in the filter $w_{21}(k)$ since the speech signal is obtained from the first channel. To begin with, we observe that the proposed MBA ideal performs significantly better than the other algorithm in all scenarios, whereas it is slightly inferior to the PSO the white noise scenario with a small filter (L=32).

In addition, the goal to investigate the potential of the MBA in terms of convergence speed in the transient regime, we have reported on the Figure 9 the temporal evolution of the SM criterion in the case of large adaptive filters (L = 128), the clean

signal is mixed with white, USASI and car noise with different input SNRs, i.e., -6 dB, 0 dB and 6 dB respectively. We can easily see that our proposed MBA needs lower time to converge in all scenarios, this means that the proposed MBA converges fast to the optimal solution in comparison with the other ones, i.e., BA, PSO and GWO algorithms. In other words, the proposed MBA has the lower steady state values in terms of SM and also the faster convergence speed performance which is a very important characteristic of any adaptive algorithm.

Table 1. The parameter setting for BA, PSO, GWO and proposed MBA algorithms.

Algorithms	Parameters
PSO (Clerc, 2010)	$maxit = 500; R = [-3, 3]^{D}$
	Population = 30; w = 2; $c_1 = 0.9$; $c_2 = 0.4$.
GWO (Okwu & Tartibu, 2021)	$maxit = 500; R = [-3,3]^{D}$; Population = 30;
BA (Yang, 2010)	$maxit = 500; R = [-3,3]^{\circ}$ Population = 30; $A_0 = 0.1; r_0 = 0.01$.
Proposed MBA [in this paper]	maxit = 500; $R = [-3,3]^{\circ}$. Population = 30; $r_0 = 0.01; \theta = 0.01; \mu = 0.04;$



Figure 8. Comparison of SM absolute final value results.



Figure 9. System misalignment criteria estimated on the adaptive filter $w_{21}(k)$ using White noise with [In left], USASI noise [In middle] and car noise [In right], with L=128 at all simulation.

4.2. Segmental signal-to-noise ratio (SegSnr) criterion evaluation

A comparison of final values of the SegSnr criterion estimated on the denoised signals $Out_1(k)$ obtained by each algorithm are shown in Figure 10. The simulation setting parameters of each algorithm are the same as those given in Table 1. The results indicate that the proposed MBA performs much better than the BA, PSO and GWO algorithms in all scenarios. We also reported in Figure 11, the temporal evolution of the SegSnr criterion obtained at the first output using an adaptive filter with length L=128. Experiments are conducted using white, USASI and car noise with different input SNRs, i.e., -6 dB, 6 dB and 6 dB respectively.

The results of Figure 11, confirm the superiority of the proposed MBA algorithm over the other ones, i.e., BA, PSO, and GWO in terms of convergence speed in transient regime as well as permanent regime in all experiments.

5. Conclusion

In this work, we have focused on the dual channel speech enhancement through adaptive filtering, we have suggested to use metaheuristic algorithms to adapt filter coefficients, also we have developed a new algorithm namely modified Bat algorithm. The proposed MBA algorithm is combined with the FBSS structure to reduce the acoustic noise components in noisy observations.

Experimental results indicate that the proposed algorithms outperform conventional and state-of-the-art metaheuristic algorithms (PSO, BA, and GWO), in terms of both convergence rate and segmental to noise ratio, as well as the steady state misalignment. In conclusion the obtained results, led us to conclude that the proposed algorithms could represent appealing solutions for speech enhancement and acoustic noise reduction applications.



Figure 10. Comparison results of final values of SegSnr criteria



Figure 11. SegSNR criteria estimated at the output signal $Out_1(n)$ values using white noise [In left], USASI noise [In middle] and car noise [In right], with L=128 at all simulation.

Conflict of interest

The authors declare that they have no conflict of interest to declare.

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